

## CHAPTER 23 (Odd)

1. a. left:  $d_1 = \frac{3}{16}'' = 0.1875'', d_2 = 1''$   
 $\text{Value} = 10^3 \times 10^{0.1875''/1''}$   
 $= 10^3 \times 1.54$   
 $= \mathbf{1.54 \text{ kHz}}$

right:  $d_1 = \frac{3}{4}'' = 0.75'', d_2 = 1''$   
 $\text{Value} = 10^3 \times 10^{0.75''/1''}$   
 $= 10^3 \times 5.623$   
 $= \mathbf{5.623 \text{ kHz}}$

b. bottom:  $d_1 = \frac{5}{16}'' = 0.3125'', d_2 = \frac{15}{16}'' = 0.9375''$   
 $\text{Value} = 10^{-1} \times 10^{0.3125''/0.9375''} = 10^{-1} \times 10^{0.333}$   
 $= 10^{-1} \times 2.153$   
 $= \mathbf{0.2153 \text{ V}}$

top:  $d_1 = \frac{11}{16}'' = 0.6875'', d_2 = 0.9375''$   
 $\text{Value} = 10^{-1} \times 10^{0.6875''/0.9375''} = 10^{-1} \times 10^{0.720}$   
 $= 10^{-1} \times 5.248$   
 $= \mathbf{0.5248 \text{ V}}$

3. a. **1000**                      b.  **$10^{12}$**                       c. **1.585**                      d. **1.096**  
 e.  **$10^{10}$**                       f. **1513.56**                      g. **10.023**                      h. **1,258,925.41**

5.  $\log_{10} 48 = \mathbf{1.681}$   
 $\log_{10} 8 + \log_{10} 6 = 0.903 + 0.778 = \mathbf{1.681}$

7.  $\log_{10} 0.5 = \mathbf{-0.301}$   
 $-\log_{10} 2 = -(0.301) = \mathbf{-0.301}$

9. a.  $\text{bels} = \log_{10} \frac{P_2}{P_1} = \log_{10} \frac{280 \text{ mW}}{4 \text{ mW}} = \log_{10} 70 = \mathbf{1.845}$

b.  $\text{dB} = 10 \log_{10} \frac{P_2}{P_1} = 10(\log_{10} 70) = 10(1.845) = \mathbf{18.45}$

11.  $\text{dB} = 10 \log_{10} \frac{P_2}{P_1} = 10 \log_{10} \frac{40 \text{ W}}{2 \text{ W}} = 10 \log_{10} 20 = \mathbf{13.01}$

13.  $\text{dB}_v = 20 \log_{10} \frac{V_2}{V_1} = 20 \log_{10} \frac{8.4 \text{ V}}{0.1 \text{ V}} = 20 \log_{10} 84 = \mathbf{38.49}$

15.  $\text{dB}_s = 20 \log_{10} \frac{P}{0.0002 \text{ } \mu\text{bar}}$   
 $\text{dB}_s = 20 \log_{10} \frac{0.001 \text{ } \mu\text{bar}}{0.0002 \text{ } \mu\text{bar}} = \mathbf{13.98}$

$$\text{dB}_s = 20 \log_{10} \frac{0.016 \mu\text{bar}}{0.0002 \mu\text{bar}} = 38.06$$

$$\text{Increase} = 24.08 \text{ dB}_s$$

$$19. \quad a. \quad A_v = \frac{V_o}{V_i} = \frac{X_C}{\sqrt{R^2 + X_C^2}} \angle -90^\circ + \tan^{-1} X_C/R = \frac{1}{\sqrt{\left[\frac{R}{X_C}\right]^2 + 1}} \angle -\tan^{-1} R/X_C$$

$$f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(2.2 \text{ k}\Omega)(0.02 \mu\text{F})} = 3617.16 \text{ Hz}$$

$$f = f_c: \quad A_v = \frac{V_o}{V_i} = 0.707$$

$$f = 0.1f_c: \quad \text{At } f_c, X_C = R = 2.2 \text{ k}\Omega$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(0.1f_c)C} = \frac{1}{0.1} \left[ \frac{1}{2\pi f_c C} \right] = 10[2.2 \text{ k}\Omega] = 22 \text{ k}\Omega$$

$$A_v = \frac{1}{\sqrt{\left[\frac{R}{X_C}\right]^2 + 1}} = \frac{1}{\sqrt{\left[\frac{2.2 \text{ k}\Omega}{22 \text{ k}\Omega}\right]^2 + 1}} = \frac{1}{\sqrt{(0.1)^2 + 1}} = 0.995$$

$$f = 0.5f_c = \frac{1}{2}f_c: \quad X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi\left[\frac{f_c}{2}\right]C} = 2 \left[ \frac{1}{2\pi f_c C} \right] = 2[2.2 \text{ k}\Omega] = 4.4 \text{ k}\Omega$$

$$A_v = \frac{1}{\sqrt{\left[\frac{2.2 \text{ k}\Omega}{4.4 \text{ k}\Omega}\right]^2 + 1}} = \frac{1}{\sqrt{(0.5)^2 + 1}} = 0.894$$

$$f = 2f_c: \quad X_C = \frac{1}{2\pi(2f_c)C} = \frac{1}{2} \left[ \frac{1}{2\pi f_c C} \right] = \frac{1}{2}[2.2 \text{ k}\Omega] = 1.1 \text{ k}\Omega$$

$$A_v = \frac{1}{\sqrt{\left[\frac{2.2 \text{ k}\Omega}{1.1 \text{ k}\Omega}\right]^2 + 1}} = \frac{1}{\sqrt{(2)^2 + 1}} = 0.447$$

$$f = 10f_c: \quad X_C = \frac{1}{2\pi(10f_c)C} = \frac{1}{10} \left[ \frac{1}{2\pi f_c C} \right] = \frac{1}{10}[2.2 \text{ k}\Omega] = 0.22 \text{ k}\Omega$$

$$A_v = \frac{1}{\sqrt{\left[\frac{2.2 \text{ k}\Omega}{0.22 \text{ k}\Omega}\right]^2 + 1}} = \frac{1}{\sqrt{(10)^2 + 1}} = 0.0995$$

$$\begin{aligned}
 \text{b. } \theta &= -\tan^{-1} R/X_C \\
 f &= f_c: \quad \theta = -\tan^{-1} 1 = -45^\circ \\
 f &= 0.1f_c: \quad \theta = -\tan^{-1} 2.2 \text{ k}\Omega / 22 \text{ k}\Omega = -\tan^{-1} \frac{1}{10} = -5.71^\circ \\
 f &= 0.5f_c: \quad \theta = -\tan^{-1} 2.2 \text{ k}\Omega / 4.4 \text{ k}\Omega = -\tan^{-1} \frac{1}{2} = -26.57^\circ \\
 f &= 2f_c: \quad \theta = -\tan^{-1} 2.2 \text{ k}\Omega / 1.1 \text{ k}\Omega = -\tan^{-1} 2 = -63.43^\circ \\
 f &= 10f_c: \quad \theta = -\tan^{-1} 2.2 \text{ k}\Omega / 0.22 \text{ k}\Omega = -\tan^{-1} 10 = -84.29^\circ
 \end{aligned}$$

$$21. \quad f_c = 500 \text{ Hz} = \frac{1}{2\pi RC} = \frac{1}{2\pi(1.2 \text{ k}\Omega)C}$$

$$C = \frac{1}{2\pi R f_c} = \frac{1}{2\pi(1.2 \text{ k}\Omega)(500 \text{ Hz})} = 0.265 \mu\text{F}$$

$$A_v = \frac{V_o}{V_i} = \frac{1}{\sqrt{\left[\frac{R}{X_C}\right]^2 + 1}}$$

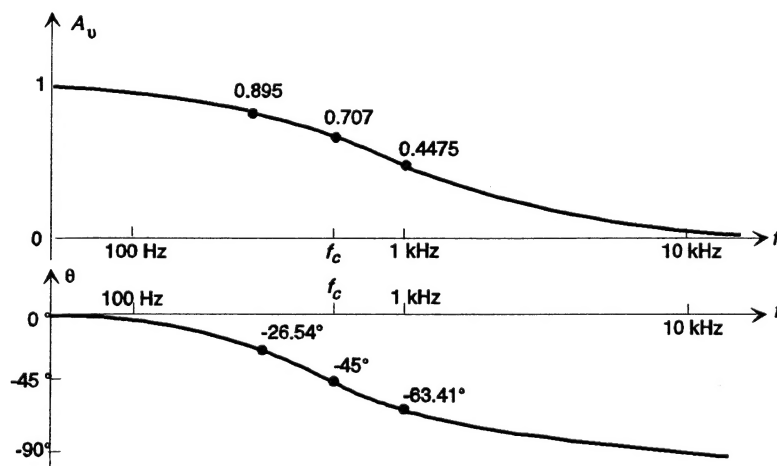
$$\text{At } f = 250 \text{ Hz}, X_C = 2402.33 \Omega \text{ and } A_v = 0.895$$

$$\text{At } f = 1000 \text{ Hz}, X_C = 600.58 \Omega \text{ and } A_v = 0.4475$$

$$\theta = -\tan^{-1} R/X_C$$

$$\text{At } f = 250 \text{ Hz} = \frac{1}{2}f_c, \theta = -26.54^\circ$$

$$\text{At } f = 1 \text{ kHz} = 2f_c, \theta = -63.41^\circ$$



23. a.  $A_v = \frac{V_o}{V_i} = \frac{R}{\sqrt{R^2 + X_C^2}} \angle \tan^{-1} X_C/R = \frac{1}{\sqrt{1 + \left(\frac{X_C}{R}\right)^2}} \angle \tan^{-1} X_C/R$

$f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(2.2 \text{ k}\Omega)(20 \text{ nF})} = 3.617 \text{ kHz}$

$f = f_c: A_v = \frac{V_o}{V_i} = 0.707$

$f = 2f_c: \text{At } f_c, X_C = R = 2.2 \text{ k}\Omega$

$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi(2f_c)C} = \frac{1}{2} \left[ \frac{1}{2\pi f_c C} \right] = \frac{1}{2}[2.2 \text{ k}\Omega] = 1.1 \text{ k}\Omega$

$A_v = \frac{1}{\sqrt{1 + \left(\frac{1.1 \text{ k}\Omega}{2.2 \text{ k}\Omega}\right)^2}} = 0.894$

$f = \frac{1}{2}f_c: X_C = \frac{1}{2\pi \left[\frac{f_c}{2}\right] C} = 2 \left[ \frac{1}{2\pi f_c C} \right] = 2[2.2 \text{ k}\Omega] = 4.4 \text{ k}\Omega$

$A_v = \frac{1}{\sqrt{1 + \left(\frac{4.4 \text{ k}\Omega}{2.2 \text{ k}\Omega}\right)^2}} = 0.447$

$f = 10f_c: X_C = \frac{1}{2\pi(10f_c)C} = \frac{1}{10} \left[ \frac{1}{2\pi f_c C} \right] = \frac{2.2 \text{ k}\Omega}{10} = 0.22 \text{ k}\Omega$

$A_v = \frac{1}{\sqrt{1 + \left(\frac{0.22 \text{ k}\Omega}{2.2 \text{ k}\Omega}\right)^2}} = 0.995$

$f = \frac{1}{10}f_c: X_C = \frac{1}{2\pi \left[\frac{f_c}{10}\right] C} = 10 \left[ \frac{1}{2\pi f_c C} \right] = 10[2.2 \text{ k}\Omega] = 22 \text{ k}\Omega$

$A_v = \frac{1}{\sqrt{1 + \left(\frac{22 \text{ k}\Omega}{2.2 \text{ k}\Omega}\right)^2}} = 0.0995$

b.  $f = f_c, \theta = 45^\circ$

$f = 2f_c, \theta = \tan^{-1} (X_C/R) = \tan^{-1} 1.1 \text{ k}\Omega/2.2 \text{ k}\Omega = \tan^{-1} \frac{1}{2} = 26.57^\circ$

$f = \frac{1}{2}f_c, \theta = \tan^{-1} \frac{4.4 \text{ k}\Omega}{2.2 \text{ k}\Omega} = \tan^{-1} 2 = 63.43^\circ$

$f = 10f_c, \theta = \tan^{-1} \frac{0.22 \text{ k}\Omega}{2.2 \text{ k}\Omega} = 5.71^\circ$

$f = \frac{1}{10}f_c, \theta = \tan^{-1} \frac{22 \text{ k}\Omega}{2.2 \text{ k}\Omega} = 84.29^\circ$

$$25. \quad A_v = \frac{V_o}{V_i} = \frac{1}{\sqrt{1 + \left(\frac{X_C}{R}\right)^2}} \angle \tan^{-1} X_C/R$$

$$f_c = \frac{1}{2\pi RC} \Rightarrow R = \frac{1}{2\pi f_c C} = \frac{1}{2\pi(2 \text{ kHz})(0.1 \mu\text{F})} = 795.77 \Omega$$

$$R = 795.77 \Omega \Rightarrow \underbrace{750 \Omega + 47 \Omega}_{\text{nominal values}} = 797 \Omega$$

$$\therefore f_c = \frac{1}{2\pi(797 \Omega)(0.1 \mu\text{F})} = 1996.93 \text{ Hz using nominal values}$$

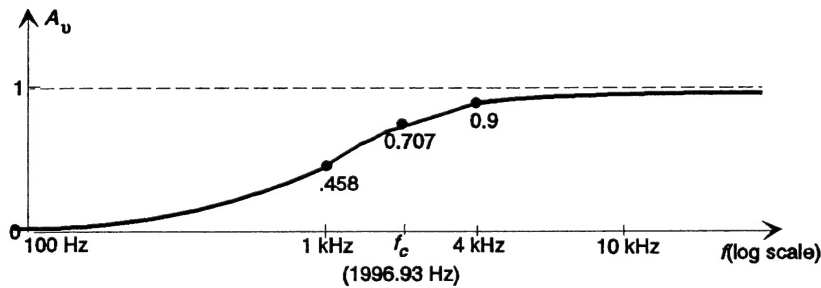
$$\text{At } f = 1 \text{ kHz, } A_v = 0.458$$

$$f = 4 \text{ kHz, } A_v \cong 0.9$$

$$\theta = \tan^{-1} \frac{X_C}{R}$$

$$f = 1 \text{ kHz, } \theta = 63.4^\circ$$

$$f = 4 \text{ kHz, } \theta = 26.53^\circ$$



$$27. \quad \text{a. low-pass section: } f_{c_1} = \frac{1}{2\pi RC} = \frac{1}{2\pi(0.1 \text{ k}\Omega)(2 \mu\text{F})} = 795.77 \text{ Hz}$$

$$\text{high-pass section: } f_{c_2} = \frac{1}{2\pi RC} = \frac{1}{2\pi(10 \text{ k}\Omega)(8 \text{ nF})} = 1989.44 \text{ Hz}$$

For the analysis to follow, it is assumed  $(R_2 + jX_{C_2}) \parallel R_1 \cong R_1$  for all frequencies of interest.

$$\text{At } f_{c_1} = 795.77 \text{ Hz:}$$

$$V_{R_1} = 0.707 V_i$$

$$X_{C_2} = \frac{1}{2\pi f C_2} = 25 \text{ k}\Omega$$

$$|V_o| = \frac{25 \text{ k}\Omega(V_{R_1})}{\sqrt{(10 \text{ k}\Omega)^2 + (25 \text{ k}\Omega)^2}} = 0.9285 V_{R_1}$$

$$V_o = (0.9285)(0.707 V_i) = 0.656 V_i$$

At  $f_{c_2} = 1989.44 \text{ Hz}$ :

$$V_o = 0.707 V_{R_1}$$

$$X_{C_1} = \frac{1}{2\pi f C_1} = 40 \Omega$$

$$|V_{R_1}| = \frac{R_1 V_i}{\sqrt{R_1^2 + X_{C_1}^2}} = \frac{100 \Omega (V_i)}{\sqrt{(100 \Omega)^2 + (40 \Omega)^2}} = 0.928 V_i$$

$$|V_o| = (0.707)(0.928 V_i) = \mathbf{0.656 V_i}$$

$$\text{At } f = 795.77 \text{ Hz} + \frac{(1989.44 \text{ Hz} - 795.77 \text{ Hz})}{2} = 1392.60 \text{ Hz}$$

$$X_{C_1} = 57.14 \Omega, X_{C_2} = 14.29 \text{ k}\Omega$$

$$V_{R_1} = \frac{100 \Omega (V_i)}{\sqrt{(100 \Omega)^2 + (57.14 \Omega)^2}} = 0.868 V_i$$

$$V_o = \frac{14.29 \text{ k}\Omega (V_{R_1})}{\sqrt{(10 \text{ k}\Omega)^2 + (14.29 \text{ k}\Omega)^2}} = 0.8193 V_{R_1}$$

$$V_o = 0.8193(0.868 V_i) = 0.711 V_i$$

$$\text{and } A_v = \frac{V_o}{V_i} = 0.711 (\cong \text{maximum value})$$

After plotting the points it was determined that the gain should also be determined at  $f = 500 \text{ Hz}$  and  $4 \text{ kHz}$ :

$$f = 500 \text{ Hz: } X_{C_1} = 159.15 \Omega, X_{C_2} = 39.8 \text{ k}\Omega,$$

$$V_{R_1} = 0.532 V_i, V_o = 0.97 V_{R_1}$$

$$V_o = \mathbf{0.516 V_i}$$

$$f = 4 \text{ kHz: } X_{C_1} = 19.89 \Omega, X_{C_2} = 4.97 \text{ k}\Omega,$$

$$V_{R_1} = 0.981 V_i, V_o = 0.445 V_{R_1}$$

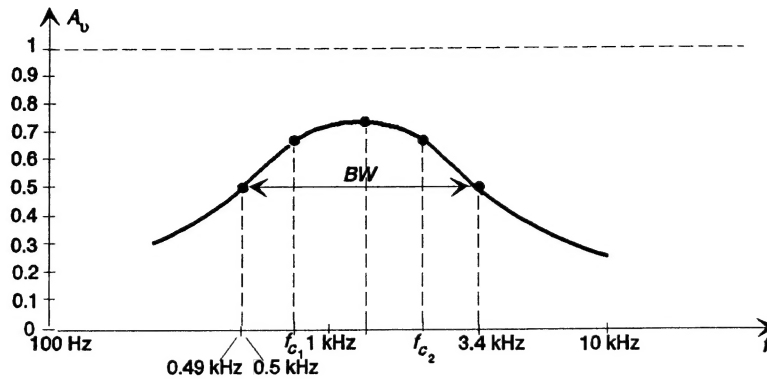
$$V_o = \mathbf{0.437 V_i}$$

b. Using  $0.707(0.711) = 0.5026 \cong 0.5$  to define the bandwidth

$$BW = 3.4 \text{ kHz} - 0.49 \text{ kHz} = 2.91 \text{ kHz}$$

$$\text{and } BW \cong \mathbf{2.9 \text{ kHz}}$$

$$\text{with } f_{\text{center}} = 490 \text{ Hz} + \left[ \frac{2.9 \text{ kHz}}{2} \right] = \mathbf{1940 \text{ Hz}}$$



29. a.  $f_s = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(5 \text{ mH})(500 \text{ pF})}} = 100.658 \text{ kHz}$

b.  $Q_s = \frac{X_L}{R + R_\ell} = \frac{2\pi(100.658 \text{ kHz})(5 \text{ mH})}{160 \Omega + 12 \Omega} = 18.39$

$BW = \frac{f_s}{Q_s} = \frac{100.658 \text{ kHz}}{18.39} = 5,473.52 \text{ Hz}$

c. At  $f = f_s$ :  $V_{o_{\max}} = \frac{R}{R + R_\ell} V_i = \frac{160 \Omega (1 \text{ V})}{172 \Omega} = 0.93 \text{ V}$  and  $A_v = \frac{V_o}{V_i} = 0.93$

Since  $Q_s \geq 10$ ,  $f_1 = f_s - \frac{BW}{2} = 100.658 \text{ kHz} - \frac{5,473.52 \text{ Hz}}{2} = 97,921.24 \text{ Hz}$

$f_2 = f_s + \frac{BW}{2} = 103,394.76 \text{ Hz}$

At  $f = 95 \text{ kHz}$ :  $X_L = 2\pi fL = 2\pi(95 \times 10^3 \text{ Hz})(5 \text{ mH}) = 2.98 \text{ k}\Omega$

$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(95 \times 10^3 \text{ Hz})(500 \text{ pF})} = 3.35 \text{ k}\Omega$

$V_o = \frac{160 \Omega (1 \text{ V} \angle 0^\circ)}{172 + j2.98 \text{ k}\Omega - j3.35 \text{ k}\Omega} = \frac{160 \text{ V} \angle 0^\circ}{172 - j370}$   
 $= \frac{160 \text{ V} \angle 0^\circ}{480 \angle -65.07^\circ} = 0.392 \text{ V} \angle 65.07^\circ$

At  $f = 105 \text{ kHz}$ :  $X_L = 2\pi fL = 2\pi(105 \text{ kHz})(5 \text{ mH}) = 3.3 \text{ k}\Omega$

$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(105 \text{ kHz})(500 \text{ pF})} = 3.03 \text{ k}\Omega$

$V_o = \frac{160 (1 \text{ V} \angle 0^\circ)}{172 + j3.3 \text{ k}\Omega - j3.03 \text{ k}\Omega} = \frac{160 \text{ V} \angle 0^\circ}{172 + j270}$   
 $= \frac{160 \text{ V} \angle 0^\circ}{320 \angle 57.50^\circ} = 0.5 \angle -57.50^\circ$

d.  $f = f_s$ :  $V_{o_{\max}} = 0.93 \text{ V}$

$f = f_1 = 97,921.24 \text{ Hz}$ ,  $V_o = 0.707(0.93 \text{ V}) = 0.658 \text{ V}$

$f = f_2 = 103,394.76 \text{ Hz}$ ,  $V_o = 0.707(0.93 \text{ V}) = 0.658 \text{ V}$

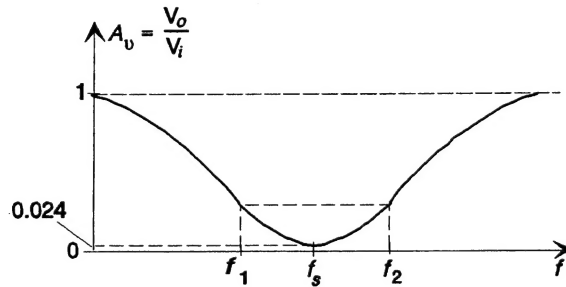
$$31. \quad a. \quad Q_s = \frac{X_L}{R + R_t} = \frac{5000 \, \Omega}{400 \, \Omega + 10 \, \Omega} = \frac{5000 \, \Omega}{410 \, \Omega} = 12.195$$

$$b. \quad BW = \frac{f_s}{Q_s} = \frac{5000 \, \text{Hz}}{12.195} = 410 \, \text{Hz}$$

$$f_1 = 5000 \, \text{Hz} - \frac{410 \, \text{Hz}}{2} = 4795 \, \text{Hz}$$

$$f_2 = 5000 \, \text{Hz} + \frac{410 \, \text{Hz}}{2} = 5205 \, \text{Hz}$$

c.



At resonance

$$V_o = \frac{10 \, \Omega (V_i)}{10 \, \Omega + 400 \, \Omega} = 0.024 \, V_i$$

$$d. \quad \text{At resonance,} \quad 10 \, \Omega \parallel 2 \, \text{k}\Omega = 9.95 \, \Omega$$

$$V_o = \frac{9.95 \, \Omega (V_i)}{9.95 \, \Omega + 400 \, \Omega} \cong 0.024 \, V_i \text{ as above!}$$

$$33. \quad a. \quad f_p = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{(400 \, \mu\text{H})(120 \, \text{pF})}} = 726.44 \, \text{kHz} \text{ (band-stop)}$$

$$X_{L_s} \angle 90^\circ + (X_{L_p} \angle 90^\circ \parallel X_C \angle -90^\circ) = 0$$

$$jX_{L_s} + \frac{(X_{L_p} \angle 90^\circ)(X_C \angle -90^\circ)}{jX_{L_p} - jX_C} = 0$$

$$jX_{L_s} + \frac{X_{L_p} X_C}{j(X_{L_p} - X_C)} = 0$$

$$jX_{L_s} - j \frac{X_{L_p} X_C}{(X_{L_p} - X_C)} = 0$$

$$X_{L_s} - \frac{X_{L_p} X_C}{X_{L_p} - X_C} = 0$$

$$X_{L_s} X_C - X_{L_s} X_{L_p} + X_{L_p} X_C = 0$$

$$\frac{\omega L_s}{\omega C} - \omega L_s \omega L_p + \frac{\omega L_p}{\omega C} = 0$$

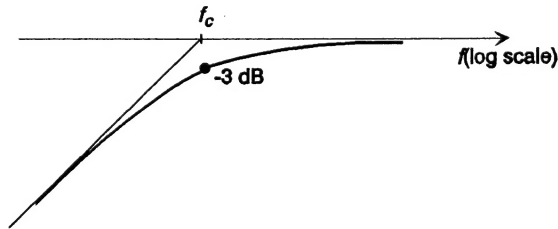


$$L_s L_p \omega^2 - \frac{1}{C} [L_s + L_p] = 0$$

$$\omega = \sqrt{\frac{L_s + L_p}{CL_s L_p}}$$

$$f = \frac{1}{2\pi} \sqrt{\frac{L_s + L_p}{CL_s L_p}} = \frac{1}{2\pi} \sqrt{\frac{460 \times 10^{-6}}{28.8 \times 10^{-19}}} = 2.013 \text{ MHz (pass-band)}$$

35. a, b.  $f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(0.47 \text{ k}\Omega)(0.05 \text{ }\mu\text{F})} = 772.55 \text{ Hz}$



c.  $f = \frac{1}{2}f_c: A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (f_c/f)^2}} = 20 \log_{10} \frac{1}{\sqrt{1 + (2)^2}} = -7 \text{ dB}$

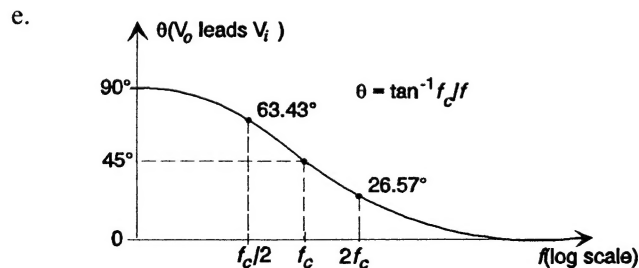
$f = 2f_c: A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (0.5)^2}} = -0.969 \text{ dB}$

$f = \frac{1}{10}f_c: A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (10)^2}} = -20.04 \text{ dB}$

$f = 10f_c: A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (0.1)^2}} = -0.043 \text{ dB}$

d.  $f = \frac{1}{2}f_c: A_v = \frac{1}{\sqrt{1 + (f_c/f)^2}} = \frac{1}{\sqrt{1 + (2)^2}} = 0.4472$

$f = 2f_c: A_v = \frac{1}{\sqrt{1 + (0.5)^2}} = 0.894$



37. a, b.  $A_v = \frac{V_o}{V_i} = A_v \angle \theta = \frac{1}{\sqrt{1 + (ff_c)^2}} \angle -\tan^{-1} ff_c$

$$f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(12 \text{ k}\Omega)(1 \text{ nF})} = 13.26 \text{ kHz}$$

c.  $f = f_c/2 = 6.63 \text{ kHz}$

$$A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (0.5)^2}} = -0.97 \text{ dB}$$

$$f = 2f_c = 26.52 \text{ kHz}$$

$$A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (2)^2}} = -6.99 \text{ dB}$$

$$f = f_c/10 = 1.326 \text{ kHz}$$

$$A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (0.1)^2}} = -0.043 \text{ dB}$$

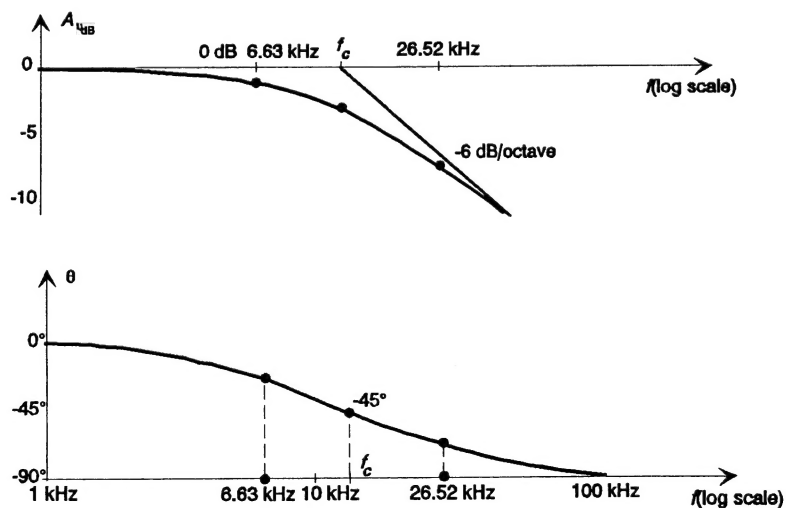
$$f = 10f_c = 132.6 \text{ kHz}$$

$$A_{v_{dB}} = 20 \log_{10} \frac{1}{\sqrt{1 + (10)^2}} = -20.04 \text{ dB}$$

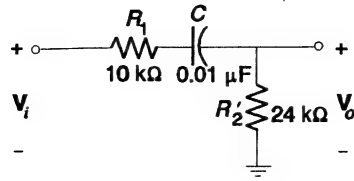
d.  $f = f_c/2$ :  $A_v = \frac{1}{\sqrt{1 + (0.5)^2}} = 0.894$

$$f = 2f_c$$
:  $A_v = \frac{1}{\sqrt{1 + (2)^2}} = 0.447$

e.  $\theta = \tan^{-1} ff_c$   
 $f = f_c/2$ :  $\theta = -\tan^{-1} 0.5 = -26.57^\circ$   
 $f = f_c$ :  $\theta = -\tan^{-1} 1 = -45^\circ$   
 $f = 2f_c$ :  $\theta = -\tan^{-1} 2 = -63.43^\circ$



39.

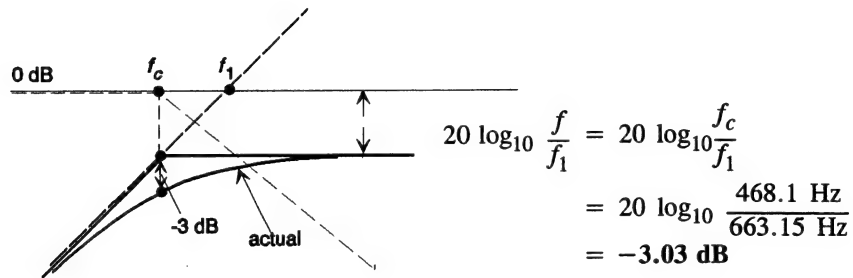


a. From Section 23.11,

$$A_v = \frac{V_o}{V_i} = \frac{jff_1}{1 + jff_c}$$

$$f_1 = \frac{1}{2\pi R_2' C} = \frac{1}{2\pi(24 \text{ k}\Omega)(0.01 \text{ }\mu\text{F})} = 663.15 \text{ Hz}$$

$$f_c = \frac{1}{2\pi(R_1 + R_2')C} = \frac{1}{2\pi(10 \text{ k}\Omega + 24 \text{ k}\Omega)(0.01 \text{ }\mu\text{F})} = 468.1 \text{ Hz}$$



b.  $\theta = 90^\circ - \tan^{-1} \frac{f}{f_1} = + \tan^{-1} \frac{f_1}{f}$

$f = f_1: \theta = 45^\circ$

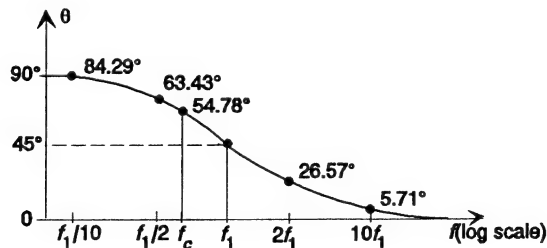
$f = f_c: \theta = 54.78^\circ$

$f = \frac{1}{2}f_1 = 331.58 \text{ Hz}, \theta = 63.43^\circ$

$f = \frac{1}{10}f_1 = 66.31 \text{ Hz}, \theta = 84.29^\circ$

$f = 2f_1 = 1,326.3 \text{ Hz}, \theta = 26.57^\circ$

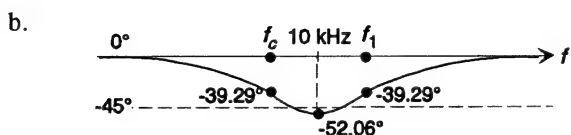
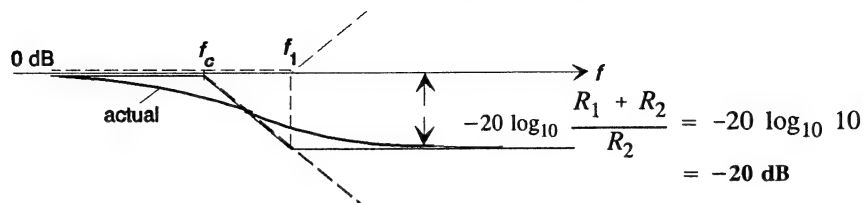
$f = 10f_1 = 6,631.5 \text{ Hz}, \theta = 5.71^\circ$



41. a. 
$$A_v = \frac{1 + j\frac{f}{f_1}}{1 + j\frac{f}{f_c}}$$

$$f_1 = \frac{1}{2\pi R_2 C} = \frac{1}{2\pi(10 \text{ k}\Omega)(800 \text{ pF})} = 19,894.37 \text{ Hz}$$

$$f_c = \frac{1}{2\pi(R_1 + R_2)C} = \frac{1}{2\pi(10 \text{ k}\Omega + 90 \text{ k}\Omega)(800 \text{ pF})} = 1,989.44 \text{ Hz}$$



$$\theta = \tan^{-1} f/f_1 - \tan^{-1} f/f_c$$

$f = 10 \text{ kHz}$

$$\theta = \tan^{-1} \frac{10 \text{ kHz}}{19.89 \text{ kHz}} - \tan^{-1} \frac{10 \text{ kHz}}{1.989 \text{ kHz}} = 26.69^\circ - 78.75^\circ = -52.06^\circ$$

$f = f_c$  ( $f_1 = 10 f_c$ )

$$\theta = \tan^{-1} \frac{f_c}{10 f_c} - \tan^{-1} \frac{f_c}{f_c} = \tan^{-1} 0.1 - \tan^{-1} 1 = 5.71^\circ - 45^\circ = -39.29^\circ$$

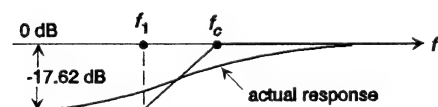
43. a. 
$$A_v = \frac{V_o}{V_i} = \frac{1 - j f_1/f}{1 - j f_c/f}$$

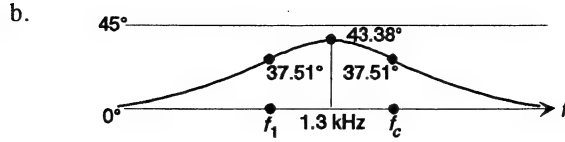
$$f_1 = \frac{1}{2\pi R_1 C} = \frac{1}{2\pi(3.3 \text{ k}\Omega)(0.05 \text{ }\mu\text{F})} = 964.58 \text{ Hz}$$

$$f_c = \frac{1}{2\pi(R_1 \parallel R_2)C} = \frac{1}{2\pi(3.3 \text{ k}\Omega \parallel 0.5 \text{ k}\Omega)(0.05 \text{ }\mu\text{F})} = 7,334.33 \text{ Hz}$$

0.434 kΩ

$$-20 \log_{10} \frac{R_1 + R_2}{R_2} = -20 \log_{10} \frac{3.3 \text{ k}\Omega + 0.5 \text{ k}\Omega}{0.5 \text{ k}\Omega} = -20 \log_{10} 7.6 = -17.62 \text{ dB}$$

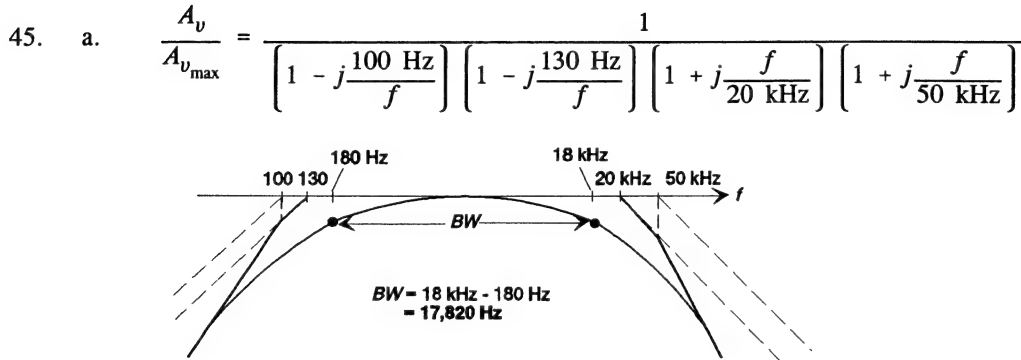




$$\theta = -\tan^{-1} \frac{f_1}{f} + \tan^{-1} \frac{f_c}{f}$$

$$f = 1.3 \text{ kHz: } \theta = -\tan^{-1} \frac{964.58 \text{ kHz}}{1.3 \text{ kHz}} + \tan^{-1} \frac{7334.33 \text{ Hz}}{1.3 \text{ kHz}}$$

$$= -36.57^\circ + 79.95^\circ = 43.38^\circ$$



Proximity of 100 Hz to 130 Hz will raise lower cutoff frequency above 130 Hz:

Testing:  $f = 180 \text{ Hz}$ : (with lower terms only)

$$A_{v_{\text{dB}}} = -20 \log_{10} \sqrt{1 + \left[\frac{100}{f}\right]^2} - 20 \log_{10} \sqrt{1 + \left[\frac{130}{f}\right]^2}$$

$$= -20 \log_{10} \sqrt{1 + \left[\frac{100}{180}\right]^2} - 20 \log_{10} \sqrt{1 + \left[\frac{130}{180}\right]^2}$$

$$= 1.17 \text{ dB} - 1.82 \text{ dB} = -2.99 \text{ dB} \cong -3 \text{ dB}$$

Proximity of 50 kHz to 20 kHz will lower high cutoff frequency below 20 kHz:

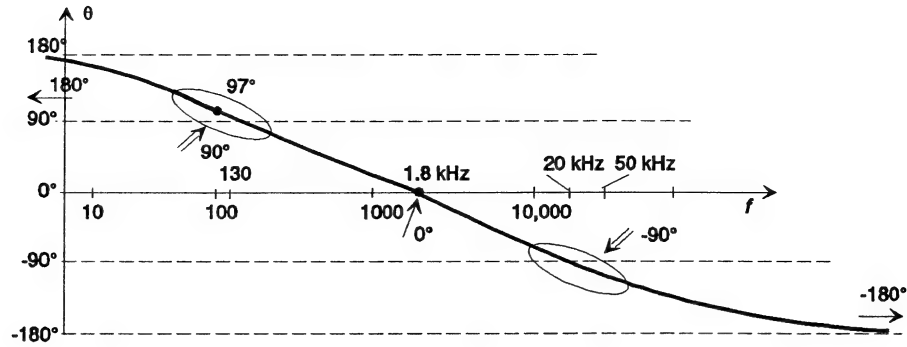
Testing:  $f = 18 \text{ kHz}$ : (with upper terms only)

$$A_{v_{\text{dB}}} = -20 \log_{10} \sqrt{1 + \left[\frac{f}{20 \text{ kHz}}\right]^2} - 20 \log_{10} \sqrt{1 + \left[\frac{f}{50 \text{ kHz}}\right]^2}$$

$$= -20 \log_{10} \sqrt{1 + \left[\frac{18 \text{ kHz}}{20 \text{ kHz}}\right]^2} - 20 \log_{10} \sqrt{1 + \left[\frac{13 \text{ kHz}}{20 \text{ kHz}}\right]^2}$$

$$= -2.576 \text{ dB} - 0.529 \text{ dB} = -3.105 \text{ dB}$$

b.

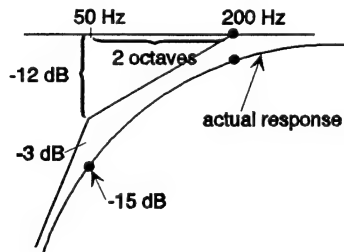


Testing:  $f = 1.8 \text{ kHz}$ :

$$\begin{aligned}\theta &= \tan^{-1} \frac{100}{1.8 \text{ kHz}} + \tan^{-1} \frac{130}{1.8 \text{ kHz}} - \tan^{-1} \frac{1.8 \text{ kHz}}{20 \text{ kHz}} - \tan^{-1} \frac{1.8 \text{ kHz}}{50 \text{ kHz}} \\ &= 3.18^\circ + 4.14^\circ - 5.14^\circ - 2.06^\circ \\ &= 0.12^\circ \approx 0^\circ\end{aligned}$$

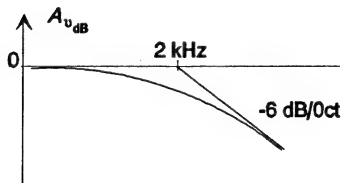
47.  $f_{\text{low}} = f_{\text{high}} - BW = 36 \text{ kHz} - 35.8 \text{ kHz} = 0.2 \text{ kHz} = 200 \text{ Hz}$

$$A_v = \frac{-120}{\left[1 - j\frac{50}{f}\right] \left[1 - j\frac{200}{f}\right] \left[1 + j\frac{f}{36 \text{ kHz}}\right]}$$



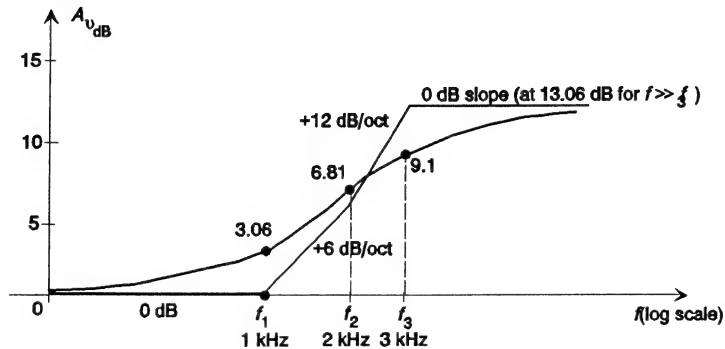
49.  $A_v = \frac{200}{200 + j0.1f} = \frac{1}{1 + j\frac{0.1f}{200}} = \frac{1}{1 + j\frac{f}{2000}}$

$$A_{v_{\text{dB}}} = 20 \log_{20} \frac{1}{\sqrt{1 + \left(\frac{f}{2000}\right)^2}}, \quad \frac{f}{2000} = 1 \text{ and } f = 2 \text{ kHz}$$



$$51. \quad A_v = \frac{\left[1 + j\frac{f}{1000}\right] \left[1 + j\frac{f}{2000}\right]}{\left[1 + j\frac{f}{3000}\right]^2}$$

$$A_{v_{dB}} = 20 \log_{10} \sqrt{1 + \left[\frac{f_1}{1000}\right]^2} + 20 \log_{10} \sqrt{1 + \left[\frac{f_2}{2000}\right]^2} + 40 \log_{10} \frac{1}{\sqrt{1 + \left[\frac{f_3}{3000}\right]^2}}$$



53. a. woofer - 400 Hz:

$$X_L = 2\pi fL = 2\pi(400 \text{ Hz})(4.7 \text{ mH}) = 11.81 \Omega$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(400 \text{ Hz})(39 \mu\text{F})} = 10.20 \Omega$$

$$R \parallel X_C = 8 \Omega \angle 0^\circ \parallel 10.20 \Omega \angle -90^\circ = 6.3 \Omega \angle -38.11^\circ$$

$$\mathbf{V}_o = \frac{(R \parallel X_C)(\mathbf{V}_i)}{(R \parallel X_C) + jX_L} = \frac{(6.3 \Omega \angle -38.11^\circ)(\mathbf{V}_i)}{(6.3 \Omega \angle -38.11^\circ) + j11.81 \Omega}$$

$$\mathbf{V}_o = 0.673 \angle -96.11^\circ \mathbf{V}_i$$

$$\text{and } A_v = \frac{V_o}{V_i} = \mathbf{0.673} \text{ vs desired } 0.707 \text{ (off by less than 5\%)}$$

tweeter - 5 kHz:

$$X_L = 2\pi fL = 2\pi(5 \text{ kHz})(0.39 \text{ mH}) = 12.25 \Omega$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(5 \text{ kHz})(2.7 \mu\text{F})} = 11.79 \Omega$$

$$R \parallel X_L = 8 \Omega \angle 0^\circ \parallel 12.25 \Omega \angle 90^\circ = 6.7 \Omega \angle 33.15^\circ$$

$$\mathbf{V}_o = \frac{(6.7 \Omega \angle 33.15^\circ)(\mathbf{V}_i)}{(6.7 \Omega \angle 33.15^\circ) - j11.79 \Omega}$$

$$\mathbf{V}_o = 0.678 \angle 88.54^\circ \mathbf{V}_i$$

$$\text{and } A_v = \frac{V_o}{V_i} = \mathbf{0.678} \text{ vs } 0.707 \text{ (off by less than 5\%)}$$

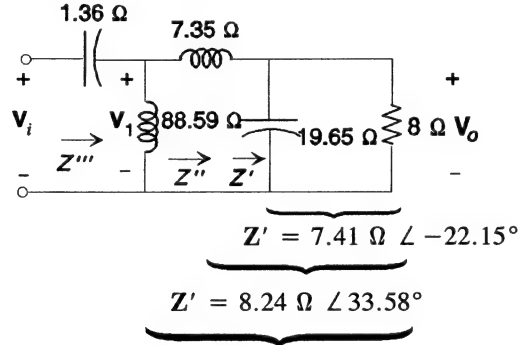
b. woofer - 3 kHz:

$$\begin{aligned}
 X_L &= 2\pi fL = 2\pi(3 \text{ kHz})(4.7 \text{ mH}) = 88.59 \, \Omega \\
 X_C &= \frac{1}{2\pi fC} = \frac{1}{2\pi(3 \text{ kHz})(39 \, \mu\text{F})} = 1.36 \, \Omega \\
 R \parallel X_C &= 8 \, \Omega \angle 0^\circ \parallel 1.36 \, \Omega \angle -90^\circ = 1.341 \, \Omega \angle -80.35^\circ \\
 V_o &= \frac{(R \parallel X_C)(V_i)}{(R \parallel X_C) + jX_L} = \frac{(1.341 \, \Omega \angle -80.35^\circ)(V_i)}{(1.341 \, \Omega \angle -80.35^\circ) + j88.59 \, \Omega} \\
 V_o &= 0.015 \angle -170.2^\circ V_i \\
 \text{and } A_v &= \frac{V_o}{V_i} = \mathbf{0.015} \text{ vs desired 0 (excellent)}
 \end{aligned}$$

tweeter - 3 kHz:

$$\begin{aligned}
 X_L &= 2\pi fL = 2\pi(3 \text{ kHz})(0.39 \text{ mH}) = 7.35 \, \Omega \\
 X_C &= \frac{1}{2\pi fC} = \frac{1}{2\pi(3 \text{ kHz})(2.7 \, \mu\text{F})} = 19.65 \, \Omega \\
 R \parallel X_L &= 8 \, \Omega \angle 0^\circ \parallel 7.35 \, \Omega \angle 90^\circ = 5.42 \, \Omega \angle 47.42^\circ \\
 V_o &= \frac{(R \parallel X_L)(V_i)}{(R \parallel X_L) + jX_C} = \frac{(5.42 \, \Omega \angle 47.42^\circ)(V_i)}{(5.42 \, \Omega \angle 47.42^\circ) - j19.65 \, \Omega} \\
 V_o &= 0.337 \angle 124.24^\circ V_i \\
 \text{and } A_v &= \frac{V_o}{V_i} = \mathbf{0.337} \text{ (acceptable since relatively close to cutoff frequency for tweeter)}
 \end{aligned}$$

c. mid-range speaker - 3 kHz:



$$\begin{aligned}
 V_1 &= \frac{Z''' V_i}{Z''' - jX_C} = \frac{(7.816 \, \Omega \angle 37.79^\circ) V_i}{7.816 \, \Omega \angle 37.79^\circ - j1.36 \, \Omega} = 1.11 \angle 8.83^\circ V_i \\
 V_o &= \frac{Z' V_1}{Z' + jX_L} = \frac{(7.41 \, \Omega \angle -22.15^\circ) V_i}{7.41 \, \Omega \angle -22.15^\circ + j7.35 \, \Omega} = 0.998 \angle -46.9^\circ V_i \\
 \text{and } A_v &= \frac{V_o}{V_i} = \mathbf{0.998} \text{ kHz (excellent)}
 \end{aligned}$$



## CHAPTER 23 (Even)

2. a. **5**                      b. **-4**                      c. **8**                      d. **-6**  
      e. **1.301**                  f. **3.937**                  g. **4.748**                  h. **-0.498**  
 4. a. **11.513**                b. **-9.21**                      c. **2.996**                      d. **9.065**

6.  $\log_{10} 0.2 = -0.699$   
 $\log_{10} 18 - \log_{10} 90 = 1.255 - 1.954 = -0.699$

8.  $\log_{10} 27 = 1.431$   
 $3 \log_{10} 3 = 3(0.4771) = 1.431$

10.  $\text{dB} = 10 \log_{10} \frac{P_2}{P_1}$   
 $6 \text{ dB} = 10 \log_{10} \frac{100 \text{ W}}{P_1}$   
 $0.6 = \log_{10} x$   
 $x = 3.981 = \frac{100 \text{ W}}{P_1}$   
 $P_1 = \frac{100 \text{ W}}{3.981} = 25.12 \text{ W}$

12.  $\text{dB}_m = 10 \log_{10} \frac{P}{1 \text{ mW}}$   
 $\text{dB}_m = 10 \log_{10} \frac{120 \text{ mW}}{1 \text{ mW}} = 10 \log_{10} 120 = 20.792$

14.  $\text{dB}_v = 20 \log_{10} \frac{V_2}{V_1}$   
 $22 = 20 \log_{10} \frac{V_o}{20 \text{ mV}}$   
 $1.1 = \log_{10} x$   
 $x = 12.589 = \frac{V_o}{20 \text{ mV}}$   
 $V_o = 251.785 \text{ mV}$

16.  $60 \text{ dB}_s \Rightarrow 90 \text{ dB}_s$   
      quiet                  loud  
 $60 \text{ dB}_s = 20 \log_{10} \frac{P_1}{0.002 \text{ } \mu\text{bar}} = 20 \log_{10} x$   
 $3 = \log_{10} x$   
 $x = 1000$

$$90 \text{ dB}_s = 20 \log_{10} \frac{P_2}{0.002 \text{ } \mu\text{bar}} = 20 \log_{10} y$$

$$4.5 = \log_{10} y$$

$$y = 31.623 \times 10^3$$

$$\frac{x}{y} = \frac{\frac{P_1}{0.002 \text{ } \mu\text{bar}}}{\frac{P_2}{0.002 \text{ } \mu\text{bar}}} = \frac{P_1}{P_2} = \frac{10^3}{31.623 \times 10^3}$$

$$\text{and } P_2 = 31.623 P_1$$

18. a.

$$8 \text{ dB} = 20 \log_{10} \frac{V_2}{0.775 \text{ V}}$$

$$0.4 = \log_{10} \frac{V_2}{0.775 \text{ V}}$$

$$\frac{V_2}{0.775 \text{ V}} = 2.512$$

$$V_2 = (2.512)(0.775 \text{ V}) = 1.947 \text{ V}$$

$$P = \frac{V^2}{R} = \frac{(1.947 \text{ V})^2}{600 \text{ } \Omega} = 6.318 \text{ mW}$$

b.

$$-5 \text{ dB} = 20 \log_{10} \frac{V_2}{0.775 \text{ V}}$$

$$-0.25 = \log_{10} \frac{V_2}{0.775 \text{ V}}$$

$$\frac{V_2}{0.775 \text{ V}} = 0.562$$

$$V_2 = (0.562)(0.775 \text{ V}) = 0.436 \text{ V}$$

$$P = \frac{V^2}{R} = \frac{(0.436 \text{ V})^2}{600 \text{ } \Omega} = 0.317 \text{ mW}$$

20. a.

$$f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(1 \text{ k}\Omega)(0.01 \text{ } \mu\text{F})} = 15.915 \text{ kHz}$$

$$f = 2f_c = 31.83 \text{ kHz}$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(31.83 \text{ kHz})(0.01 \text{ } \mu\text{F})} = 500 \text{ } \Omega$$

$$A_v = \frac{V_o}{V_i} = \frac{X_C}{\sqrt{R^2 + X_C^2}} = \frac{500 \text{ } \Omega}{\sqrt{(1 \text{ k}\Omega)^2 + (0.5 \text{ k}\Omega)^2}} = 0.4472$$

$$V_o = 0.4472 V_i = 0.4472(10 \text{ mV}) = 4.472 \text{ mV}$$

b.

$$f = \frac{1}{10} f_c = \frac{1}{10}(15,915 \text{ kHz}) = 1.5915 \text{ kHz}$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(1.5915 \text{ kHz})(0.01 \text{ } \mu\text{F})} = 10 \text{ k}\Omega$$

$$A_v = \frac{V_o}{V_i} = \frac{X_C}{\sqrt{R^2 + X_C^2}} = \frac{10 \text{ k}\Omega}{\sqrt{(1 \text{ k}\Omega)^2 + (10 \text{ k}\Omega)^2}} = 0.995$$

$$V_o = 0.995 V_i = 0.995(10 \text{ mV}) = 9.95 \text{ mV}$$

- c. Yes, at  $f = f_c$ ,  $V_o = 7.07 \text{ mV}$   
 at  $f = \frac{1}{10}f_c$ ,  $V_o = 9.95 \text{ mV}$  (much higher)  
 at  $f = 2f_c$ ,  $V_o = 4.472 \text{ mV}$  (much lower)

22. a.  $f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(4.7 \text{ k}\Omega)(500 \text{ pF})} = 67.726 \text{ kHz}$

b.  $f = 0.1 f_c = 0.1(67.726 \text{ kHz}) \cong 6.773 \text{ kHz}$   
 $X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(6.773 \text{ kHz})(500 \text{ pF})} = 46.997 \text{ k}\Omega$   
 $A_v = \frac{V_o}{V_i} = \frac{X_C}{\sqrt{R^2 + X_C^2}} = \frac{46.997 \text{ k}\Omega}{\sqrt{(4.7 \text{ k}\Omega)^2 + (46.997 \text{ k}\Omega)^2}} = 0.995 \cong 1$

c.  $f = 10f_c = 677.26 \text{ kHz}$   
 $X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(677.26 \text{ kHz})(500 \text{ pF})} \cong 470 \text{ }\Omega$   
 $A_v = \frac{V_o}{V_i} = \frac{X_C}{\sqrt{R^2 + X_C^2}} = \frac{470 \text{ }\Omega}{\sqrt{(4.7 \text{ k}\Omega)^2 + (470 \text{ }\Omega)^2}} = 0.0995 \cong 0.1$

d.  $A_v = \frac{V_o}{V_i} = 0.01 = \frac{X_C}{\sqrt{R^2 + X_C^2}}$   
 $\sqrt{R^2 + X_C^2} = \frac{X_C}{0.01} = 100 X_C$   
 $R^2 + X_C^2 = 10^4 X_C^2$   
 $R^2 = 10^4 X_C^2 - X_C^2 = 9,999 X_C^2$   
 $X_C = \frac{R}{\sqrt{9,999}} = \frac{4.7 \text{ k}\Omega}{99.995} \cong 47 \text{ }\Omega$   
 $X_C = \frac{1}{2\pi fC} \Rightarrow f = \frac{1}{2\pi X_C C} = \frac{1}{2\pi(47 \text{ }\Omega)(500 \text{ pF})} = 6.77 \text{ MHz}$

24. a.  $f = f_c: A_v = \frac{V_o}{V_i} = 0.707$

b.  $f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(10 \text{ k}\Omega)(1000 \text{ pF})} = 15.915 \text{ kHz}$   
 $f = 4f_c = 4(15.915 \text{ kHz}) = 63.66 \text{ kHz}$   
 $X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(63.66 \text{ kHz})(1000 \text{ pF})} = 2.5 \text{ k}\Omega$   
 $A_v = \frac{V_o}{V_i} = \frac{R}{\sqrt{R^2 + X_C^2}} = \frac{10 \text{ k}\Omega}{\sqrt{(10 \text{ k}\Omega)^2 + (2.5 \text{ k}\Omega)^2}} = 0.970 \text{ (significant rise)}$

$$c. \quad f = 100f_c = 100(15.915 \text{ kHz}) = 1591.5 \text{ kHz} \cong 1.592 \text{ MHz}$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(1.592 \text{ MHz})(1000 \text{ pF})} = 99.972 \text{ } \Omega$$

$$A_v = \frac{R}{\sqrt{R^2 + X_C^2}} = \frac{10 \text{ k}\Omega}{\sqrt{(10 \text{ k}\Omega)^2 + (99.972 \text{ } \Omega)^2}} = 0.99995 \cong 1$$

$$d. \quad \text{At } f = f_c, V_o = 0.707V_i = 0.707(10 \text{ mV}) = 7.07 \text{ mV}$$

$$P_o = \frac{V_o^2}{R} = \frac{(7.07 \text{ mV})^2}{10 \text{ k}\Omega} \cong 5 \text{ nW}$$

$$26. \quad a. \quad f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi(100 \text{ k}\Omega)(20 \text{ pF})} = 79.577 \text{ kHz}$$

$$b. \quad f = 0.01f_c = 0.01(79.577 \text{ kHz}) = 0.7958 \text{ kHz} \cong 796 \text{ Hz}$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(796 \text{ Hz})(20 \text{ pF})} = 9.997 \text{ M}\Omega$$

$$A_v = \frac{V_o}{V_i} = \frac{R}{\sqrt{R^2 + X_C^2}} = \frac{100 \text{ k}\Omega}{\sqrt{(100 \text{ k}\Omega)^2 + (9.997 \text{ M}\Omega)^2}} = 0.01 \cong 0$$

$$c. \quad f = 100f_c = 100(79.577 \text{ kHz}) \cong 7.96 \text{ MHz}$$

$$X_C = \frac{1}{2\pi fC} = \frac{1}{2\pi(7.96 \text{ MHz})(20 \text{ pF})} = 999.72 \text{ } \Omega$$

$$A_v = \frac{V_o}{V_i} = \frac{R}{\sqrt{R^2 + X_C^2}} = \frac{100 \text{ k}\Omega}{\sqrt{(100 \text{ k}\Omega)^2 + (999.72 \text{ } \Omega)^2}} = 0.99995 \cong 1$$

$$d. \quad A_v = \frac{V_o}{V_i} = 0.5 = \frac{R}{\sqrt{R^2 + X_C^2}}$$

$$\sqrt{R^2 + X_C^2} = 2R$$

$$R^2 + X_C^2 = 4R^2$$

$$X_C^2 = 4R^2 - R^2 = 3R^2$$

$$X_C = \sqrt{3R^2} = \sqrt{3}R = \sqrt{3}(100 \text{ k}\Omega) = 173.2 \text{ k}\Omega$$

$$X_C = \frac{1}{2\pi fC} \Rightarrow f = \frac{1}{2\pi X_C C} = \frac{1}{2\pi(173.2 \text{ k}\Omega)(20 \text{ pF})}$$

$$f = 45.95 \text{ kHz}$$

$$28. \quad f_1 = \frac{1}{2\pi R_1 C_1} = 4 \text{ kHz}$$

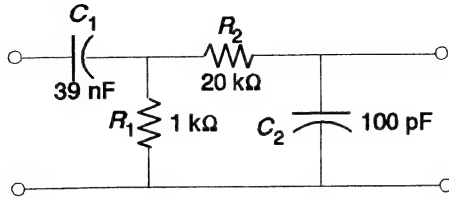
$$\text{Choose } R_1 = 1 \text{ k}\Omega$$

$$C_1 = \frac{1}{2\pi f_1 R_1} = \frac{1}{2\pi(4 \text{ kHz})(1 \text{ k}\Omega)} = 39.8 \text{ nF} \therefore \text{Use } 39 \text{ nF}$$

$$f_2 = \frac{1}{2\pi R_2 C_2} = 80 \text{ kHz}$$

Choose  $R_2 = 20 \text{ k}\Omega$

$$C_2 = \frac{1}{2\pi f_2 R_2} = \frac{1}{2\pi(80 \text{ kHz})(20 \text{ k}\Omega)} = 99.47 \text{ pF} \therefore \text{Use } 100 \text{ pF}$$



$$\text{Center frequency} = 4 \text{ kHz} + \frac{80 \text{ kHz} - 4 \text{ kHz}}{2} = 42 \text{ kHz}$$

At  $f = 42 \text{ kHz}$ ,  $X_{C_1} = 97.16 \Omega$ ,  $X_{C_2} = 37.89 \text{ k}\Omega$

Assuming  $Z_2 \gg Z_1$

$$|V_{R_1}| = \frac{R_1(V_i)}{\sqrt{R_1^2 + X_{C_1}^2}} = 0.995 V_i$$

$$|V_o| = \frac{X_{C_2}(V_{R_1})}{\sqrt{R_2^2 + X_{C_2}^2}} = 0.884 V_i$$

$$V_o = 0.884 V_{R_1} = 0.884(0.995 V_i) = \mathbf{0.88 V_i}$$

as  $f = f_1$ :  $V_{R_1} = 0.707 V_i$ ,  $X_{C_2} = 221.05 \text{ k}\Omega$

and  $V_o = 0.996 V_{R_1}$

so that  $V_o = 0.996 V_{R_1} = 0.996(0.707 V_i) = 0.704 V_i$

Although  $A_v = 0.88$  is less than the desired level of 1,  $f_1$  and  $f_2$  do define a band of frequencies for which  $A_v \geq 0.7$  and the power to the load is significant.

$$30. \quad a. \quad f_p = \frac{1}{2\pi\sqrt{LC}} \sqrt{1 - \frac{R_\ell^2 C}{L}} \cong \mathbf{159.15 \text{ kHz}}$$

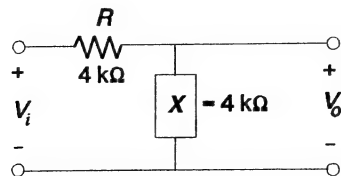
$$Q_\ell = \frac{X_L}{R_\ell} = \frac{2\pi f_p L}{R_\ell} = \frac{2\pi(159.15 \text{ kHz})(1 \text{ mH})}{16 \Omega} = 62.5 \gg 10$$

$$\therefore Z_{T_p} = Q_\ell^2 R_\ell = (62.5)^2 16 \Omega = 62.5 \text{ k}\Omega \gg R = 4 \text{ k}\Omega$$

and  $V_o \cong V_i$  at resonance.

However,  $R = 4 \text{ k}\Omega$  affects the shape of the resonance curve and  $BW = f_p/Q_\ell$  cannot be applied.

For  $A_v = \frac{V_o}{V_i} = 0.707$ ,  $|X| = R$  for the following configuration



For frequencies near  $f_p$ ,  $X_L \gg R_\ell$  and  $Z_L = R_\ell + jX_L \cong X_L$   
and  $X = X_L \parallel X_C$ .

For frequencies near  $f_p$  but less than  $f_p$

$$X = \frac{X_C X_L}{X_C - X_L}$$

and for  $A_v = 0.707$

$$\frac{X_C X_L}{X_C - X_L} = R$$

Substituting  $X_C = \frac{1}{2\pi f_1 C}$  and  $X_L = 2\pi f_1 L$   
the following equation can be derived:

$$f_1^2 + \frac{1}{2\pi RC} f_1 - \frac{1}{4\pi^2 LC} = 0$$

For this situation:

$$\frac{1}{2\pi RC} = \frac{1}{2\pi(4 \text{ k}\Omega)(0.001 \text{ }\mu\text{F})} = 39.79 \times 10^3$$

$$\frac{1}{4\pi^2 LC} = \frac{1}{4\pi^2(1 \text{ mH})(0.001 \text{ }\mu\text{F})} = 2.53 \times 10^{10}$$

and solving the quadratic equation,  $f_1 = 140.4 \text{ kHz}$

and  $\frac{BW}{2} = 159.15 \text{ kHz} - 140.4 \text{ kHz} = 18.75 \text{ kHz}$   
with  $BW = 2(18.75 \text{ kHz}) = 37.5 \text{ kHz}$

b.  $Q_p = \frac{f_p}{BW} = \frac{159.15 \text{ kHz}}{37.5 \text{ kHz}} = 4.24$

32. a.  $Q_\ell = \frac{X_L}{R_\ell} = \frac{400 \text{ }\Omega}{10 \text{ }\Omega} = 40$

$$Z_{T_p} = Q_\ell^2 R_\ell = (40)^2 20 \text{ }\Omega = 32 \text{ k}\Omega \gg 1 \text{ k}\Omega$$

At resonance,  $V_o = \frac{32 \text{ k}\Omega V_i}{32 \text{ k}\Omega + 1 \text{ k}\Omega} = 0.97 V_i$

and  $A_v = \frac{V_o}{V_i} = 0.97$

For the low cutoff frequency note solution to Problem 30:

$$f_1^2 + \frac{1}{2\pi f R_C} f_1 - \frac{1}{4\pi^2 LC} = 0$$

$$C = \frac{1}{2\pi f X_C} = \frac{1}{2\pi(20 \text{ kHz})(400 \text{ }\Omega)} = 19.9 \text{ nF}$$

$$L = \frac{X_L}{2\pi f} = \frac{400 \text{ }\Omega}{2\pi(20 \text{ kHz})} = 3.18 \text{ mH}$$

Substituting into the above equation and solving

$$f_1 = 16.4 \text{ kHz}$$

$$\text{with } \frac{BW}{2} = 20 \text{ kHz} - 16.4 \text{ kHz} = 3.6 \text{ kHz}$$

$$\text{and } BW = 2(3.6 \text{ kHz}) = 7.2 \text{ kHz}$$

$$Q_p = \frac{f_p}{BW} = \frac{20 \text{ kHz}}{7.2 \text{ kHz}} = 2.78$$

b. —

c. At resonance

$$Z_{T_p} = 32 \text{ k}\Omega \parallel 100 \text{ k}\Omega = 24.24 \text{ k}\Omega$$

$$\text{with } V_o = \frac{24.24 \text{ k}\Omega V_i}{24.24 \text{ k}\Omega + 1 \text{ k}\Omega} = 0.96V_i$$

$$\text{and } A_v = \frac{V_o}{V_i} = 0.96 \text{ vs } 0.97 \text{ above}$$

At frequencies to the right and left of  $f_p$ , the impedance  $Z_{T_p}$  will decrease and be affected less and less by the parallel  $100 \text{ k}\Omega$  load. The characteristics, therefore, are only slightly affected by the  $100 \text{ k}\Omega$  load.

d. At resonance

$$Z_{T_p} = 32 \text{ k}\Omega \parallel 20 \text{ k}\Omega = 12.31 \text{ k}\Omega$$

$$\text{with } V_o = \frac{12.31 \text{ k}\Omega V_i}{12.31 \text{ k}\Omega + 1 \text{ k}\Omega} = 0.925V_i \text{ vs } 0.97 \text{ above}$$

At frequencies to the right and left of  $f_p$ , the impedance of each frequency will actually be less due to the parallel  $20 \text{ k}\Omega$  load. The effect will be to narrow the resonance curve and decrease the bandwidth with an increase in  $Q_p$ .

34. a.  $f_s = \frac{1}{2\pi\sqrt{LC}} \Rightarrow L_s = \frac{1}{4\pi^2 f_s^2 C} = \frac{1}{4\pi^2 (100 \text{ kHz})^2 (200 \text{ pF})} = 12.68 \text{ mH}$

$$X_L = 2\pi f L = 2\pi (30 \text{ kHz})(12.68 \text{ mH}) = 2388.91 \Omega$$

$$X_C = \frac{1}{2\pi f C} = \frac{1}{2\pi (30 \text{ kHz})(200 \text{ pF})} = 26.54 \text{ k}\Omega$$

$$X_C - X_L = 26.54 \text{ k}\Omega - 2388.91 \Omega = 24.15 \text{ k}\Omega(C)$$

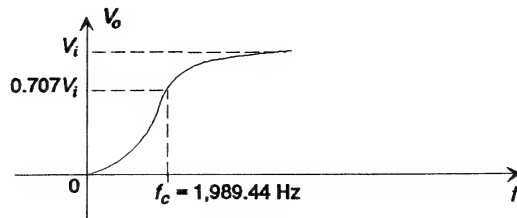
$$X_{L_p} = X_{C(\text{net})} = 24.15 \text{ k}\Omega$$

$$L_p = \frac{X_L}{2\pi f} = \frac{24.15 \text{ k}\Omega}{2\pi (30 \text{ kHz})} = 128.19 \text{ mH}$$

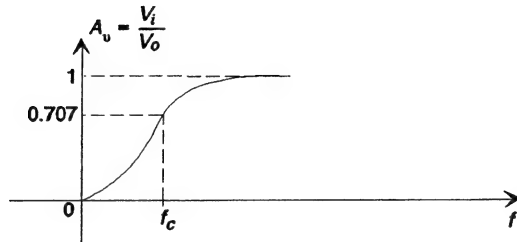
36. a.  $f_c = \frac{1}{2\pi RC} = \frac{1}{2\pi (6 \text{ k}\Omega \parallel 12 \text{ k}\Omega) 0.01 \mu\text{F}} = \frac{1}{2\pi (4 \text{ k}\Omega) (0.01 \mu\text{F})} = 1989.44 \text{ Hz}$

$$\frac{V_o}{V_i} = \frac{1}{\sqrt{1 + (f_c/f)^2}}$$

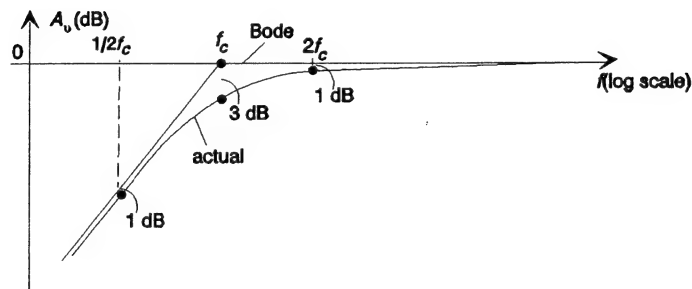
$$\text{and } V_o = \left[ \frac{1}{\sqrt{1 + (f_c/f)^2}} \right] V_i$$



b.



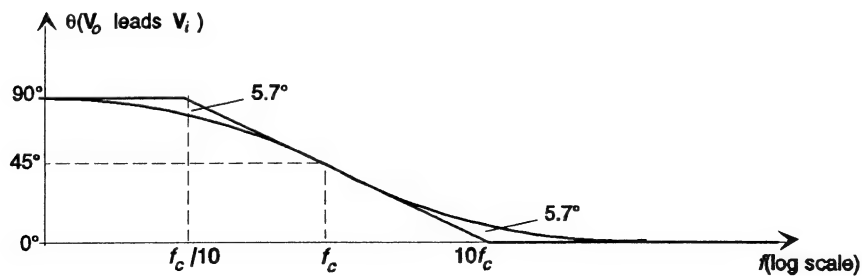
c. & d.



e. Remember the log scale!  $1.5f_c$  not midway between  $f_c$  and  $2f_c$

$$\begin{aligned} A_{v_{\text{dB}}} &= 20 \log_{10} A_v \\ -1.5 &= 20 \log_{10} A_v \\ -0.075 &= \log_{10} A_v \\ A_v &= \frac{V_o}{V_i} = \mathbf{0.841} \end{aligned}$$

f.  $\theta = \tan^{-1} f_c/f$





$$\begin{aligned}
38. \quad a. \quad R_2 \parallel X_C &= \frac{(R_2)(-jX_C)}{R_2 - jX_C} = -j \frac{R_2 X_C}{R_2 - jX_C} \\
V_o &= \frac{\left[ \frac{-jR_2 X_C}{R_2 - jX_C} \right] V_i}{R_1 - j \frac{R_2 X_C}{R_2 - jX_C}} = -j \frac{R_2 X_C V_i}{R_1(R_2 - jX_C) - jR_2 X_C} \\
&= \frac{-jR_2 X_C V_i}{R_1 R_2 - jR_1 X_C - jR_2 X_C} = \frac{-jR_2 X_C V_i}{R_1 R_2 - j(R_1 + R_2)X_C} \\
&= \frac{R_2 X_C V_i}{jR_1 R_2 + (R_1 + R_2)X_C} = \frac{R_2 V_i}{j \frac{R_1 R_2}{X_C} + (R_1 + R_2)} \\
&= \frac{R_2 V_i}{R_1 + R_2 + j \frac{R_1 R_2}{X_C}} = \frac{\left[ \frac{R_2}{R_1 + R_2} \right] V_i}{1 + j \left[ \frac{R_1 R_2}{R_1 + R_2} \right] \frac{1}{X_C}}
\end{aligned}$$

$$\text{and } A_v = \frac{V_o}{V_i} = \frac{\frac{R_2}{R_1 + R_2}}{1 + j\omega \left[ \frac{R_1 R_2}{R_1 + R_2} \right] C}$$

$$\text{or } A_v = \frac{R_2}{R_1 + R_2} \left[ \frac{1}{1 + j2\pi f(R_1 \parallel R_2)C} \right]$$

$$\text{defining } f_c = \frac{1}{2\pi(R_1 \parallel R_2)C}$$

$$A_v = \frac{R_2}{R_1 + R_2} \left[ \frac{1}{1 + jff_c} \right]$$

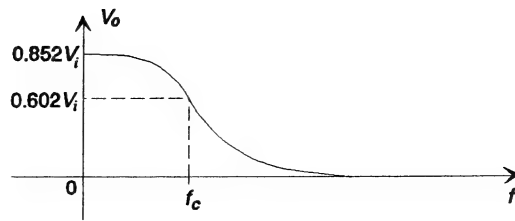
$$\text{and } A_v = \frac{R_2}{R_1 + R_2} \left[ \frac{1}{\sqrt{1 + (ff_c)^2}} \angle -\tan^{-1} ff_c \right]$$

$$\text{with } |V_o| = \frac{R_2}{R_1 + R_2} \left[ \frac{1}{\sqrt{1 + (ff_c)^2}} \right] |V_i|$$

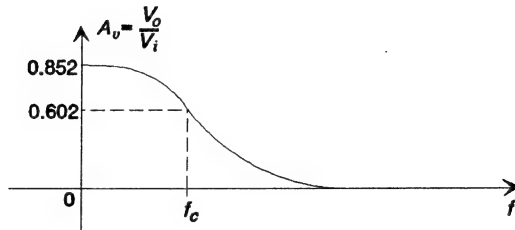
$$\text{for } f \ll f_c, V_o = \frac{R_2}{R_1 + R_2} V_i = \frac{27 \text{ k}\Omega}{4.7 \text{ k}\Omega + 27 \text{ k}\Omega} V_i = 0.852 V_i$$

$$\text{at } f = f_c: V_o = 0.852[0.707] V_i = 0.602 V_i$$

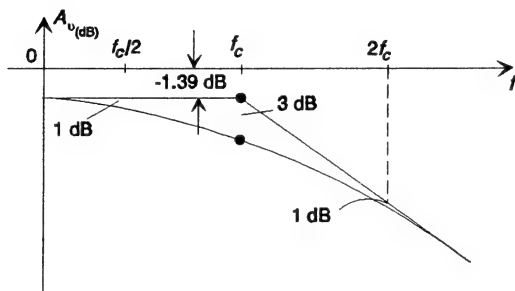
$$f_c = \frac{1}{2\pi(R_1 \parallel R_2)C} = 994.72 \text{ Hz}$$



b.



c. & d.

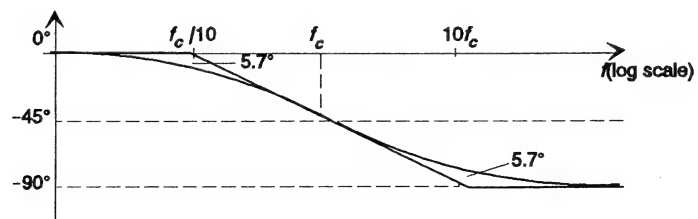


$$\begin{aligned} -20 \log_{10} \frac{R_1 + R_2}{R_2} &= -20 \log_{10} \frac{4.7 \text{ k}\Omega + 27 \text{ k}\Omega}{27 \text{ k}\Omega} \\ &= -20 \log_{10} 1.174 = -1.39 \text{ dB} \end{aligned}$$

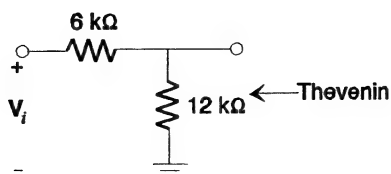
e.  $A_{v_{\text{dB}}} \cong -1.39 \text{ dB} - 0.5 \text{ dB} = -1.89 \text{ dB}$

$$\begin{aligned} A_{v_{\text{dB}}} &= 20 \log_{10} A_v \\ -1.89 &= 20 \log_{10} A_v \\ 0.0945 &= \log_{10} A_v \\ A_v &= \frac{V_o}{V_i} = \mathbf{0.804} \end{aligned}$$

f.  $\theta = -\tan^{-1} f/f_c$

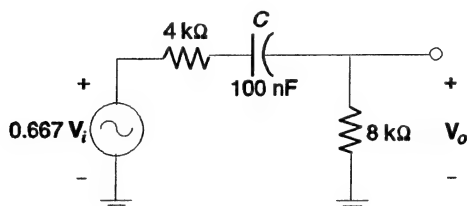


40. a.



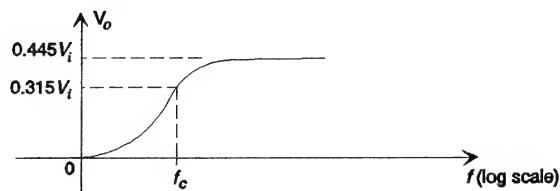
$$V_{Th} = \frac{12 \text{ k}\Omega}{12 \text{ k}\Omega + 6 \text{ k}\Omega} V_i = 0.667 V_i$$

$$R_{Th} = 6 \text{ k}\Omega \parallel 12 \text{ k}\Omega = 4 \text{ k}\Omega$$



$f = \infty \text{ Hz}$ : ( $C \Rightarrow$  short circuit)

$$V_o = \frac{8 \text{ k}\Omega}{8 \text{ k}\Omega + 4 \text{ k}\Omega} (0.667 V_i) = 0.445 V_i$$



$$\text{voltage-divider rule: } V_o = \frac{R_2(0.667 V_i)}{R_1 + R_2 - jX_C} = \frac{0.667 R_2 V_i}{R_1 + R_2 - jX_C}$$

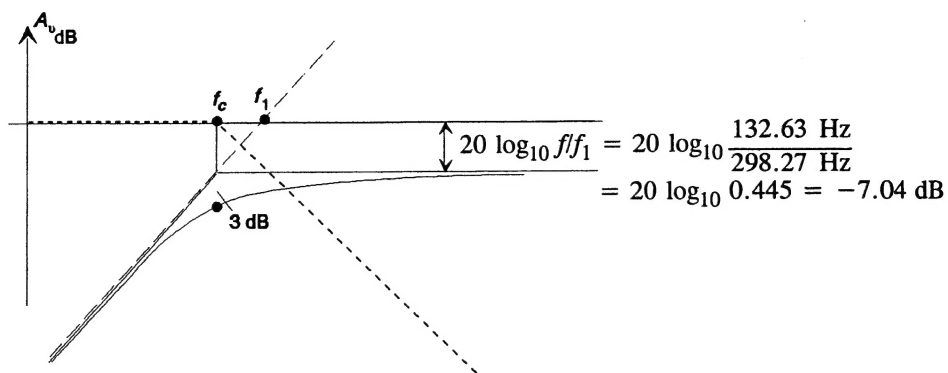
$$\text{and } A_v = \frac{V_o}{V_i} = \frac{0.667 R_2}{R_1 + R_2 - jX_C} = \frac{j2\pi f(0.667 R_2)C}{1 + j2\pi f(R_1 + R_2)C}$$

$$\text{so that } A_v = \frac{jff_1}{1 + jff_c} \text{ with } f_1 = \frac{1}{2\pi(0.667 R_2)C} = \frac{1}{2\pi(0.667)(8 \text{ k}\Omega)(100 \text{ nF})}$$

$$= 298.27 \text{ Hz}$$

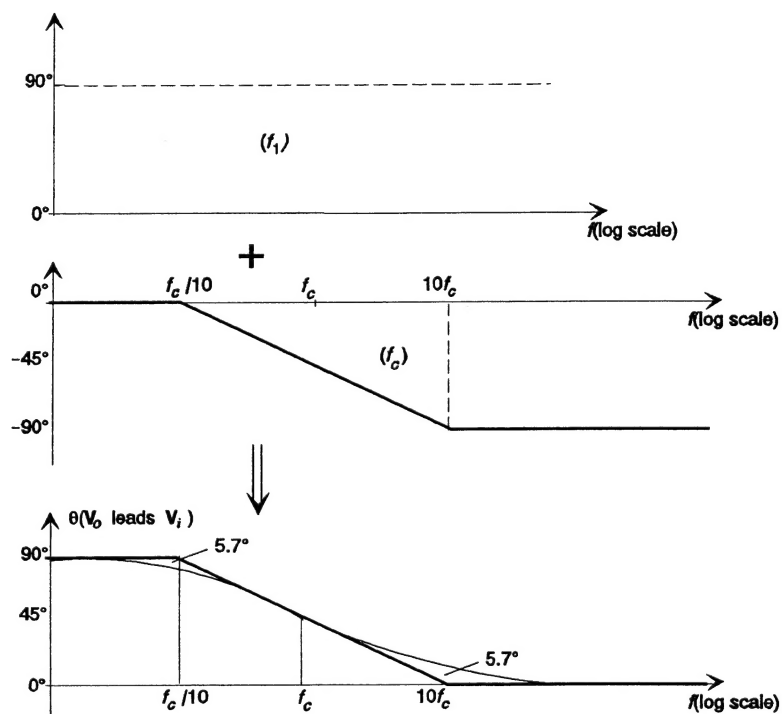
$$\text{and } f_c = \frac{1}{2\pi(R_1 + R_2)C} = \frac{1}{2\pi(4 \text{ k}\Omega + 8 \text{ k}\Omega)(100 \text{ nF})}$$

$$= 132.63 \text{ Hz}$$



b.  $\theta = 90^\circ - \tan^{-1} f/f_c = +\tan^{-1} f_c/f = \tan^{-1} 132.6 \text{ Hz}/f$

or



42. a.  $R_1$  no effect!  
Note Section 23.12.

$$A_v = \frac{V_o}{V_i} = \frac{1 + j(f/f_1)}{1 + j(f/f_c)}$$

$$f_1 = \frac{1}{2\pi(6 \text{ k}\Omega)(0.01 \text{ }\mu\text{F})} = 2652.58 \text{ Hz}$$

$$f_c = \frac{1}{2\pi(12 \text{ k}\Omega + 6 \text{ k}\Omega)(0.01 \text{ }\mu\text{F})} = 884.19 \text{ Hz}$$

Note Fig. 23.65.

Asymptote at 0 dB from  $0 \rightarrow f_c$   
 $-6 \text{ dB/octave}$  from  $f_c$  to  $f_1$   
 $-9.54 \text{ dB}$  from  $f_1$  on  $\left[ -20 \log \frac{12 \text{ k}\Omega + 6 \text{ k}\Omega}{6 \text{ k}\Omega} = -9.54 \text{ dB} \right]$

(b) Note Fig. 23.67.

From  $0^\circ$  to  $-26.50^\circ$  at  $f_c$  and  $f_1$   
 $\theta = \tan^{-1} f/f_1 - \tan^{-1} f/f_c$   
 At  $f = 1500 \text{ Hz}$  (between  $f_c$  and  $f_1$ )  
 $\theta = \tan^{-1} 1500 \text{ Hz}/2652.58 \text{ Hz} - \tan^{-1} 1500 \text{ Hz}/884.19 \text{ Hz}$   
 $= 29.49^\circ - 59.48^\circ = -30^\circ$

44. a. Note Section 23.13.

$$A_v = \frac{1 - j(f_1/f)}{1 - j(f_c/f)}$$

$$f_1 = \frac{1}{2\pi R_1 C} = \frac{1}{2\pi (3.3 \text{ k}\Omega)(0.05 \text{ }\mu\text{F})} = 964.58 \text{ Hz}$$

$$f_c = \frac{1}{2\pi (R_1 \parallel R_2) C} = \frac{1}{2\pi (3.3 \text{ k}\Omega \parallel 0.5 \text{ k}\Omega) 0.05 \text{ }\mu\text{F}} = 7334.33 \text{ Hz}$$

$0.434 \text{ k}\Omega$

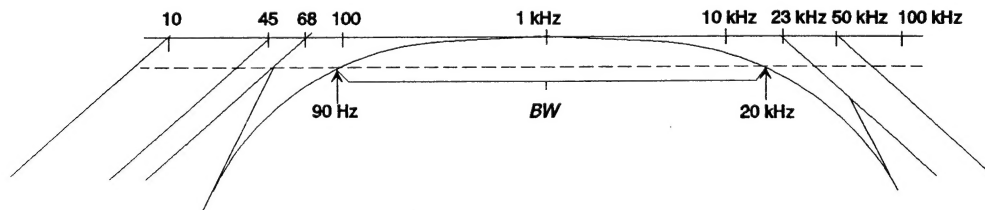
Note Fig. 23.72.

$$-20 \log_{10} \frac{R_1 + R_2}{R_2} = -20 \log_{10} \frac{3.3 \text{ k}\Omega + 0.5 \text{ k}\Omega}{0.5 \text{ k}\Omega} = -17.62 \text{ dB}$$

Asymptote at  $-17.62 \text{ dB}$  from  $0 \rightarrow f_1$   
 $+6 \text{ dB/octave}$  from  $f_1$  to  $f_c$   
 $0 \text{ dB}$  from  $f_c$  on

b.  $\theta = -\tan^{-1} f_1/f + \tan^{-1} f_c/f$   
 Test at  $3 \text{ kHz}$   
 $\theta = -\tan^{-1} 964.58 \text{ Hz}/3.0 \text{ kHz} + \tan^{-1} 7334.33 \text{ Hz}/3.0 \text{ kHz}$   
 $= -17.82^\circ + 67.75^\circ = 49.93^\circ \cong 50^\circ$

Therefore rising above  $45^\circ$  at and near the peak



50 kHz vs 23 kHz  $\rightarrow$  drop about 1 dB at 23 kHz due to 50 kHz break.  
 Ignore effect of break frequency at 10 Hz.  
 Assume  $-2 \text{ dB}$  drop at 68 Hz due to break frequency at 45 Hz.  
 Rough sketch suggests low cut-off frequency of 90 Hz.

Checking: Ignoring upper terms

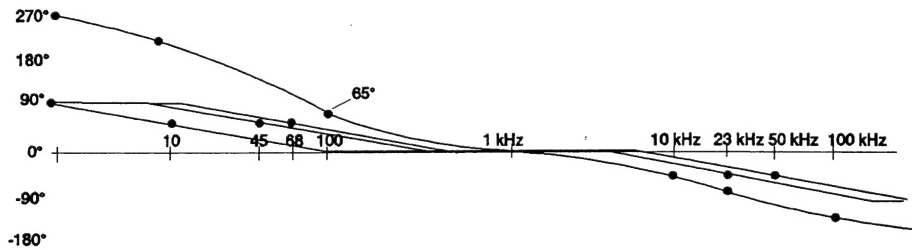
$$\begin{aligned}
 A'_{v_{dB}} &= -20 \log_{10} \left[ 1 + \left( \frac{10 \text{ Hz}}{f} \right)^2 \right] - 20 \log_{10} \left[ 1 + \left( \frac{45 \text{ Hz}}{f} \right)^2 \right] - 20 \log_{10} \left[ 1 + \left( \frac{68 \text{ Hz}}{f} \right)^2 \right] \\
 &= -0.0532 \text{ dB} - 0.969 \text{ dB} - 1.96 \text{ dB} \\
 &= -2.98 \text{ dB} \quad (\text{excellent})
 \end{aligned}$$

High frequency cutoff: Try 20 kHz

$$\begin{aligned}
 A'_{v_{dB}} &= -20 \log_{10} \left[ 1 + \left( \frac{f}{23 \text{ kHz}} \right)^2 \right] - 20 \log_{10} \left[ 1 + \left( \frac{f}{50 \text{ kHz}} \right)^2 \right] \\
 &= -2.445 \text{ dB} - 0.6445 \text{ dB} \\
 &= -3.09 \text{ dB} \quad (\text{excellent})
 \end{aligned}$$

$\therefore BW = 20 \text{ kHz} - 90 \text{ Hz} = 19,910 \text{ Hz} \cong 20 \text{ kHz}$

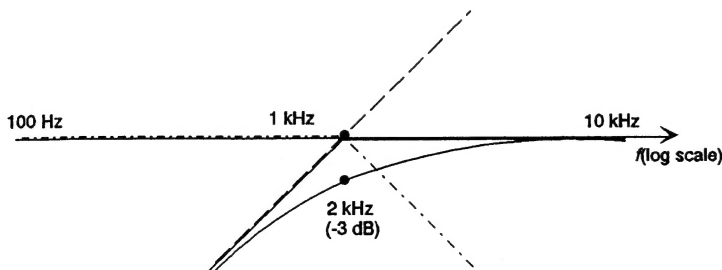
$f_1 = 90 \text{ Hz}, f_2 = 20 \text{ kHz}$



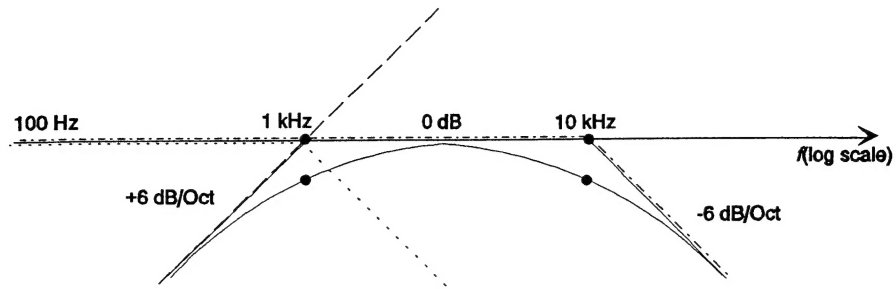
Testing:  $f = 100 \text{ Hz}$

$$\begin{aligned}
 \theta &= \tan^{-1} \frac{10 \text{ Hz}}{f} + \tan^{-1} \frac{45 \text{ Hz}}{f} + \tan^{-1} \frac{68 \text{ Hz}}{f} - \tan^{-1} \frac{f}{23 \text{ kHz}} - \tan^{-1} \frac{f}{50 \text{ kHz}} \\
 &= \tan^{-1} 0.1 + \tan^{-1} 0.45 + \tan^{-1} 0.68 - \tan^{-1} 0.00435 - \tan^{-1} .002 \\
 &= 5.71^\circ + 24.23^\circ + 34.22^\circ - 0.249^\circ - 0.115^\circ \\
 &= 63.8^\circ \text{ vs about } 65^\circ \text{ on the plot}
 \end{aligned}$$

$$\begin{aligned}
 48. \quad A_v &= \frac{0.05}{0.05 - j \frac{100}{f}} = \frac{1}{1 - j \frac{100}{0.05 f}} = \frac{1}{1 - j \frac{2000}{f}} = \frac{+jf}{+jf + 2000} \\
 &= \frac{+j \frac{f}{2000}}{1 + j \frac{f}{2000}} \text{ and } f_1 = 2000 \text{ Hz}
 \end{aligned}$$



50. 
$$A_v = \frac{jf/1000}{(1 + jf/1000)(1 + jf/10,000)}$$



52. 
$$\frac{j\omega}{1000} = j \frac{2\pi f}{1000} = j \frac{f}{\frac{1000}{2\pi}} = j \frac{f}{159.16 \text{ Hz}}, \quad \frac{j\omega}{5000} = j \frac{f}{\frac{5000}{2\pi}} = j \frac{f}{795.78 \text{ Hz}}$$

